Intermediate Algebra Skill Builder # PF – 6A Factoring Quadratic Trinomials with Leading Coefficient Different from 1 *ac* – Method: GROUPING

A quadratic trinomial with leading coefficient different from 1 looks like

$$ax^2 + bx + c$$
.

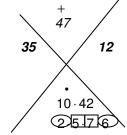
To factor such a trinomial by grouping:

- **a.** Find two numbers that multiply to *ac* and that add up to the middle coefficient *b*.
 - **b.** Rewrite the middle term using the two numbers found in Step a.
 - **c.** Factor by grouping.

Examples

1.
$$10x^2 + 47x + 42$$

Solution:



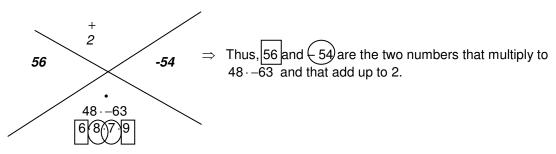
⇒ Thus, 35 and 12 are the two numbers that multiply to 10.42 and that add up to 47.

Rewrite $10x^2 + 47x + 42$ as $10x^2 + 35x + 12x + 42$ and factor by grouping:

$$(10x^{2}+35x)+(12x+42)$$

= 5x(2x+7)+6(2x+7)
= (2x+7)(5x+6)

2. $48x^2 + 2x - 63$



Rewrite $48x^2 + 2x - 63$ as $48x^2 + 56x - 54x - 63$ and factor by grouping:

$$(48x^{2} + 56x) + (-54x - 63)$$

= 8x(6x+7) - 9(6x+7)
= (6x+7)(8x-9)

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Factor the given quadratic trinomial.

| 1. $15x^2 + 38x + 24$ | 2. | $24x^2 - 50x + 25$ |
|------------------------------|----|--------------------|
|------------------------------|----|--------------------|

3. $32x^2 + 52x - 45$ **4.** $35x^2 + 48x - 27$

5. $40y^2 - 37y - 63$

6. $16y^2 - 62y + 55$

7. $33t^2 + 67t - 56$ **8.** $96t^2 + 116t - 65$

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Answers

| 1. | (3x+4)(5x+6) | 5. $(8y+7)(5y-9)$ |
|----|--------------|--------------------------|
| 2. | (4x-5)(6x-5) | 6. $(2y-5)(8y-11)$ |
| 3. | (8x-5)(4x+9) | 7. $(3t+8)(11t-7)$ |
| 4. | (7x-3)(5x+9) | 8. $(12t-5)(8t+13)$ |
| | | |

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